# A Multi-level Sketch-based Interface for Decorative Pattern Exploration 

## Supplementary File: Methodology Details

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## Shape Feature

When computing the distance between two Tensor descriptors, the empty cells of the input sketch are masked off. Since a sketch is usually much simpler than decorative images, this method can avoid the tendency for images that are as sparse as the sketch.

## Reflection feature

Denoting the reflection feature of the input sketch as $V_{\text {sketch }}\left\{v_{1}, v_{2}, \ldots\right\}$, the minimum distance between a unit vector $v \in V_{\text {sketch }}$ and another reflection feature $V_{\text {image }}$ is

$$
f\left(v, V_{\text {image }}\right)=\min _{v_{k} \in V_{\text {image }}} \angle\left(v, v_{k}\right),
$$

where $\angle(\because, \cdot)$ maps the angle between two vectors to $[0, \pi / 2]$, and the result is set as the maximum $\pi / 2$ if $V_{\text {image }}$ is a null set. The sum of such minimum distances represents the distance from $V_{\text {sketch }}$ to $V_{\text {image }}$, vice versa. Therefore, the distance between two reflection features is defined as

$$
D_{\text {ref }}=\sum_{\hat{v} \in V_{\text {sketch }}} f\left(\hat{v}, V_{\text {image }}\right)+\sum_{v \in V_{\text {image }}} f\left(v, V_{\text {sketch }}\right) \cdot(1-\alpha \beta)
$$

where $\alpha=0.5$ in our implementation.
Rotation feature
Denoting the specified rotation feature as $C_{\text {sketch }}$ and another feature as $C_{\text {image }}$, the two rotation symmetries are hierarchical if

$$
C_{\text {sketch }} \bmod C_{\text {image }}=0
$$

## Translation feature

Denoting the translation feature as $T_{\text {sketch }}\left\{v_{1}, v_{2}, \ldots\right\}$, the distance between it and another translation feature $T_{\text {image }}$ is represented as

$$
D_{\text {trans }}=\sum_{\widehat{v}_{l} \in T_{\text {sketch }}}\left[\min _{v_{j} \in T_{\text {image }}} \angle\left(\widehat{v}_{l}, v_{j}\right)+\omega| | \widehat{v}_{l}\left|-\left|v_{j}\right|\right|\right]+\lambda \sum_{v \in T_{\text {image }}} f\left(v, T_{\text {sketch }}\right),
$$

where the weight $\lambda=0.3$ in our implementation and $\omega$ is a binary number which equals to 1 when a lattice is sketched.

